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**Reihe Ökonomie  
Economics Series**

# **Pension Reform and Labor Market Incentives**

**Walter H. Fisher, Christian Keuschnigg**



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Founded in 1963 by two prominent Austrians living in exile – the sociologist Paul F. Lazarsfeld and the economist Oskar Morgenstern – with the financial support from the Ford Foundation, the Austrian Federal Ministry of Education and the City of Vienna, the Institute for Advanced Studies (IHS) is the first institution for postgraduate education and research in economics and the social sciences in Austria. The **Economics Series** presents research done at the Department of Economics and Finance and aims to share “work in progress” in a timely way before formal publication. As usual, authors bear full responsibility for the content of their contributions.

Das Institut für Höhere Studien (IHS) wurde im Jahr 1963 von zwei prominenten Exilösterreichern – dem Soziologen Paul F. Lazarsfeld und dem Ökonomen Oskar Morgenstern – mit Hilfe der Ford-Stiftung, des Österreichischen Bundesministeriums für Unterricht und der Stadt Wien gegründet und ist somit die erste nachuniversitäre Lehr- und Forschungsstätte für die Sozial- und Wirtschaftswissenschaften in Österreich. Die **Reihe Ökonomie** bietet Einblick in die Forschungsarbeit der Abteilung für Ökonomie und Finanzwirtschaft und verfolgt das Ziel, abteilungsinterne Diskussionsbeiträge einer breiteren fachinternen Öffentlichkeit zugänglich zu machen. Die inhaltliche Verantwortung für die veröffentlichten Beiträge liegt bei den Autoren und Autorinnen.

## **Abstract**

This paper investigates how parametric reform in a pay-as-you-go pension system with a tax benefit link affects retirement incentives and work incentives of prime-age workers. We find that postponed retirement tends to harm incentives of prime-age workers in the presence of a tax benefit link, thereby creating a policy trade-off in stimulating aggregate labor supply. We show how several popular reform scenarios are geared either towards young or old workers, or, indeed, both groups under appropriate conditions. We also provide a sharp characterization of the excess burden of pension insurance and show how it depends on the behavioral supply elasticities on the extensive and intensive margins and the effective tax rates implicit in contribution rates.

## **Keywords**

Pension reform, retirement, hours worked, tax benefit link, actuarial adjustment, excess burden

## **JEL Classification**

H55, J26

**Comments**

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# 1 Introduction

In light of the concerns faced by policy makers regarding the long-run funding of public pensions, many countries have initiated reforms. Apart from the need to restore sustainability of pension systems, these reforms are importantly motivated by the concerns about the potentially adverse consequences of existing systems for labor market incentives. For these reasons, most countries have initiated reforms that i) strengthen the tax-benefit link by, for instance, bringing more people into a harmonized pension system in which pensions are assessed on the basis of past earnings; and ii) introduce more actuarial fairness in order to provide disincentives, or “penalties”, for early retirement and to improve the incentives for labor market participation of older workers nearing retirement. It has been long recognized that the tax character of pension contributions tends to discourage work effort of the actively employed (intensive labor supply). This has led policy makers to propose a tighter tax-benefit link to reduce distortions in the labor supply decision faced by younger workers. More recently, the date, or timing, of the retirement decision has received increasing attention. To raise the average retirement age, recent reforms often include adjustments of the pension size to provide stronger incentives for continued work (extensive labor supply).

What is less well-known are the important interactions between the incentives facing younger and older workers. Rewarding late retirement might have quite adverse consequences for implicit taxes faced by younger workers. While some approaches to pension reform might succeed in strengthening labor supply on both margins, by encouraging work effort of younger workers and simultaneously participation of older workers, other scenarios might encourage one margin at the expense of the other, with possibly no clear cut net effect on aggregate labor supply. The goal of this paper is, then, to develop a formal model that helps to clarify how incentives of young and old workers interact and how pension reform might give rise to off-setting, or mutually, reinforcing effects on aggregate labor supply.

There is a large literature on pension economics and old age insurance; see, for example,

Feldstein and Liebman (2002), Bovenberg (2003), Lindbeck and Persson (2003) and Fenge and Pestieau (2005) for a few important reviews.

The recent policy debate in the U.S. has focussed to a great extent on the choice between increased capital funding [e.g. Kotlikoff (1997), Feldstein (2005a,b), and Feldstein and Samwick (2002)] versus parametric reform of existing pay-as-you-go (PAYG) systems [e.g. Diamond (2004), Diamond and Orszag (2005)]. Apart from its impact on national savings, the potential labor market implications of public pensions have always played an important role in this debate. An on-going concern is the effect on intensive labor supply, i.e. hours worked by the active generation. The crucial question is to which extent the contributions to social security are actually perceived as a tax by the active generation. The answer depends, of course, on the institutional design of the PAYG system. In a system with a tax-benefit link in which pensions are based on past earnings, the effective tax rate may be roughly half of the statutory contribution rate, as recent calculations for Germany by Fenge and Werding (2004) have shown. Beginning with Feldstein and Samwick (1972), the existing literature has calculated a much higher tax component for young workers far from retirement, while the effective tax is, in contrast, much lower for workers nearing retirement. Disney (2004) provided recent calculations of the effective tax rates implied by PAYG contributions and econometric estimates of the employment effects. The results are consistent with usual findings of the empirical literature on intensive labor supply, namely that male employment is not particularly responsive to tax incentives, while women's activity rates are highly adversely affected by the effective contribution tax.

According to the influential studies of Gruber and Wise (1999a, 1999b, 2002), a serious problem associated with PAYG systems is that they impose significant disincentives to work at older ages. Gruber and Wise (2005) provide calculations for the relationship between later retirement and the amount of additional benefits that lead to actuarial fairness. Börsch-Supan (2000, 2003) provides evidence on participation decision of older workers for Germany. Scarpetta (1996) finds empirical evidence supporting this phenom-

enon in a cross-country study. A major factor behind the “trend” toward early retirement in developed economies is that existing PAYG systems distort the labor supply decision on the extensive margin and thereby encourage early retirement. Blöndal and Scarpetta (1998) suggest that early retirement provisions in many countries have led to a dramatic decrease in the labor force participation among older workers. The fact that benefits are not adjusted in an actuarially fair manner is a key reason for this large distortion on the extensive margin. Theoretical work on the implications of social security for the retirement decision is inspired by the seminal contributions of Feldstein (1974) and Diamond and Mirrlees (1978). More recent theoretical contributions on the (optimal) design of pension systems in the presence of a retirement decision is found, for example, in Cremer and Pestieau (2003) and Cremer, Lozachmeur and Pestieau (2004).<sup>1</sup>

The novel contribution of this paper is to shed more light on how the structure of existing PAYG pension systems simultaneously affect the intensive and extensive margins in different ways. In particular, the paper will show how the effective tax rates on intensive labor supply of younger workers and the participation tax rate of older workers, and therefore the extensive and intensive labor supply responses, importantly interact with each other, depending on the specific institutional design of the system. We are able to provide a sharper characterization of the excess burden of a PAYG pension system that brings out the parallels with the recent literature, found in Kleven and Kreiner (2006), Immervoll et al. (2007) and Saez (2002), on labor taxation in the presence of intensive and extensive supply. We show how the excess burden depends i) on the behavioral elasticities with respect to prime-age labor supply and the retirement decision of older workers and ii) on the effective tax rates for these two groups. We then turn to parametric pension reform and derive the behavioral response and welfare implications of strengthening the tax-benefit link and introducing more actuarial fairness by making the pension eligibility rules more sensitive to the choice of the retirement date. These are important reform strategies chosen by numerous countries in the recent past. To our knowledge, a rigorous

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<sup>1</sup>See Fenge and Pestieau (2005) for a review of this work.

analysis of a marginal reform of the tax-benefit link by making it more sensitive with respect to retirement age is also novel.

To focus on the essential mechanisms, the model we consider is a simple one. Agents are risk neutral, live two periods, make an intensive labor supply decision when young and an extensive, participation choice in the second period of life. Production technology is Ricardian and labor markets are competitive. Consumer-workers make their choices subject to a general pension earnings rule that conveniently parameterizes different degrees of actuarial fairness and encompasses the most important specifications of actual pension systems: i) a Beveridge-type system in which “flat” old-age earnings are independent of contributions; ii) a Bismarckian PAYG system that incorporates a constant tax-benefit link, although one that is not sensitive to the chosen retirement age and is, thus, unfair in an actuarial sense; iii) a modified PAYG system that adjusts actuarially the pension rule according to the participation decision in the sense of Gruber-Wise; and iv) a fully-funded system in which contributions earn the market rate of interest and pension earnings are adjusted to take into account the length of the retirement period.

The rest of the paper is organized as follows: section 2 describes the households and their intensive and extensive labor supply decisions in view of the structure of the PAYG system. This part of the paper also outlines the equilibrium OLG structure and calculates the responses of intensive and extensive work effort to a socioeconomic trend toward early retirement, including its impact on the pension system. In section 3, we introduce the welfare measure, compute the consequences of a higher statutory contribution rate, and characterize the marginal excess burden resulting from the expansion of the system. Section 4 is devoted to parametric pension reform including several scenarios of strengthening the tax-benefit link and introducing a greater degree of actuarial fairness. The paper closes in section 5 with a brief summary.

## 2 The Model

### 2.1 Households

In order to concentrate on labor market behavior of young and old workers, we keep the macroeconomic framework as simple as possible. Regarding representative consumer-workers, we assume they live two periods and are risk neutral. Leaving aside issues related to savings, we make the simplifying assumption that present and future consumption,  $C_t$ ,  $t = 1, 2$ , are perfect substitutes.

In other words, agents care only about the present value and not the timing of consumption. In assuming a Ricardian framework, labor productivity is the same in both periods and is fixed at unity. With competitive labor markets, the (real) wage is also unity,  $MPL = W = 1$ , and there is no unemployment.<sup>2</sup> We specify further that agents face the choice of how hard to work when young and when to retire when old. The former is an intensive labor supply decision,  $L$ , while the extensive labor supply margin reflects a discrete participation decision of whether to work at all. The retirement date is denoted by  $x$  and corresponds to the share of the overall old age period spent in active employment. First and second period budgets are

$$C_1 = (1 - \tau)WL - S, \quad C_2 = x \cdot (1 - \tau)W + (1 - x) \cdot P + RS, \quad (1)$$

where  $S$  is savings,  $\tau$  is the statutory contribution rate to the pension system,  $P$  represents pension earnings, and  $R (\equiv 1 + r)$  is the (constant) interest factor. During the second period of life, the agent continues working for a share  $x$  of the entire period and retires for the remaining part  $1 - x$ . We refer to the variable  $x$  as the retirement date. Upon retirement, wage earnings are replaced by pension income. To further simplify, we assume that labor supply in the second period is fixed.

Life-time utility of an agent is of the usual intertemporally separable form. For simplicity, we exclude income effects on labor supply and additionally assume that consumption

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<sup>2</sup>We retain in this section the symbol  $W$  for expositional convenience.

and work effort are separable within each period,

$$V = C_1 - \varphi(L) + \frac{1}{R} \cdot [C_2 - \beta\phi(x)], \quad (2)$$

where the parameter  $\beta$  scales the preference for early versus late retirement. Disutility of work effort  $\varphi(L)$  when young and of continued employment  $\phi(x)$  during old age are convex increasing, i.e. the derivatives  $\varphi'$ ,  $\varphi''$ ,  $\phi'$ ,  $\phi''$  are all positive. Given that present and future consumption are perfect substitutes, the interest rate must be equal to the rate of time preference and is, thus, exogenous.

Since it is crucial in analyzing alternative pension policies, we must describe in detail the factors influencing pension earnings,  $P$ . They are given by

$$P = m(x) [\tau \cdot WL \cdot R^p + \tau \cdot Wx] + B, \quad (3)$$

where  $B$  is a “flat” pension payment independent of contributions. The pension system might pay interest on contributions, which is reflected in the factor  $R^p$ . The key relationship in our analysis is the conversion factor  $m(x)$  that scales contributions from past earnings into a pension entitlement. It reflects the tax-benefit link that can be actuarially adjusted depending on old-age labor market participation, or retirement, decision  $x$ . The specification (3) encompasses several distinct pension regimes: i) a Beveridge-type system ( $m(x) = 0$ ) in which “flat” old-age earnings are independent of contributions,  $P = B$ ; ii) a Bismarckian PAYG system that incorporates a constant tax-benefit link,  $m(x) = m_0 > 0$ , with  $B = 0$  and  $R^p = 1$ . If the conversion factor does *not* increase in the retirement date, the system remains unfair in the sense that pension adjustment does not reflect the length of the remaining life-time  $1 - x$ ; iii) a modified PAYG system with an actuarial adjustment of pensions conditional on the retirement date (“Gruber-Wise” incentives),  $m'(x) > 0$ ; and iv) a fully-funded system in which contributions earn the market rate of interest,  $R^p = R$ , and pension earnings are adjusted to take into account the length of the retirement period so that  $m(x) = 1/(1 - x)$ .<sup>3</sup>

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<sup>3</sup>As Feldstein (2005a) points out, the absence of a tax-benefit link implies that an agent’s contributions represent a 100% tax rate. Regarding PAYG systems with a tax-benefit link, Fenge and Werding (2003) provide evidence that approximately 50% of contributions in Germany are effectively taxed.

To model the implications of a number of structural pension reforms, we assume that the tax-benefit link  $m(x)$  takes the specification

$$m = m(x) = \frac{\alpha}{1-x} + m_0, \quad \alpha > 0, \quad (4)$$

which embeds an actuarial adjustment component  $(\alpha/1-x)$  and a constant term  $m_0$  scaling the tax-benefit link. Actuarial adjustment is partial if  $0 < \alpha < 1$  and complete if  $\alpha = 1$ . Given (3)–(4), the Bismarck-type pension equals  $P = m_0\tau[L+x]W$ , while its fully capital funded counterpart is  $P = (1-x)^{-1}\tau[L \cdot R + x]W$ , with  $B = m_0 = 0$ . Substituting the pension formula of the funded system into the budget identities of the agent shows that life-time wealth is independent of the parameters of the pension system, i.e.  $C_1 + C_2/R = WL + xW/R$ . The fully funded system provides a perfect substitute for private savings in this framework.

Substituting the budget identities into the value function  $V$  yields the problem

$$V = \max_{L,x} (1-\tau)WL - \varphi(L) + \frac{1}{R}[x(1-\tau)W + (1-x)P - \beta\phi(x)], \quad (5)$$

subject to  $P$  determined by (3)–(4). The optimality condition with respect to a young worker's labor supply decision is

$$\varphi'(L) = (1-\tau_L)W, \quad \tau_L = \tau \cdot [1 - (1-x)m \cdot R^p/R] < \tau, \quad (6)$$

where  $\tau_L$  is the implicit tax rate on first-period employment  $L$  in the sense of Feldstein and Samwick (1992). It will be discussed more fully below. The participation, or retirement, decision of an older worker is governed by

$$\beta\phi'(x) = (1-\tau)W - P + (1-x)\frac{\partial P}{\partial x}, \quad (7)$$

where the derivative in the last term,

$$\frac{\partial P}{\partial x} = \tau \cdot [m' \cdot (LR^p + x) + m]W, \quad (8)$$

reflects the effect on pension earnings of choosing a longer working life  $x$ . Since (6)–(8), together with the economy's resource constraints, determine the equilibrium response of workers to pension policy, it is important to analyze these conditions in more detail.

## 2.2 Intensive Labor Supply

Observe in (6) that the implicit tax  $\tau_L$  on intensive labor supply is *less* than the statutory rate  $\tau$ . In a system with a tax-benefit link, pensions are assessed on the basis of past wage earnings. Greater work effort by the young therefore raises not only their current income, but also leads to higher retirement income when old. This means that not all of the contribution rate is perceived as a “pure” tax, since agents foresee an individual return in terms of a higher pension entitlement accruing in the retirement period  $1 - x$ . Moreover, the simple relationship in (6) contains the essential insights regarding intensive labor supply.

First, when contributions earn no interest ( $R^p = 1$ ) under a PAYG system, future benefits are discounted by the market interest rate. The younger an agent, the more distant are future pensions, and, hence, the larger is the discounting. For this reason, empirical calculations, such as in Feldstein and Samwick (1992) or Fenge and Werding (2003), show that implicit tax rates tend to be rather high for younger workers and fall as the retirement date approaches. Second, if the retirement age  $x$  increases, pensions are consumed for a smaller remaining retirement period. If the conversion factor is not increased simultaneously, a higher retirement age raises implicit tax rates on the young and lead to a larger distortion of intensive labor supply. Third, the formula nests the extreme cases of flat PAYG (Beveridge) and fully funded systems. In a flat system without any tax-benefit link,  $m = 0$ , pension contributions are effectively taxed at the statutory rate,  $\tau_L = \tau$ . In contrast,  $\tau_L$  is zero under the fully funded system. The fully funded system pays full interest on contributions,  $R^p = R$ , and also adjusts pension size in an actuarially fair way,  $m = (1 - x)^{-1}$ , to take account of the length of the remaining retirement period. Note that a Gruber-Wise adjustment for late retirement adjusts the conversion factor in a similar way and, hence, reduces the implicit tax on young workers. However, since contributions earn no interest, this adjustment is not sufficient to entirely eliminate the implicit tax on the young.

Calculating the intensive labor supply response in (6) in terms of proportional rates



of change yields

$$\hat{L} = -\sigma \cdot \hat{\tau}_L, \quad \sigma \equiv \varphi'/(L\varphi'') > 0, \quad (9)$$

where  $\hat{\tau}_L \equiv d\tau_L/(1 - \tau_L)$  and  $\sigma$  is the (constant) net wage elasticity of work effort.<sup>4</sup> Clearly, a rise in the implicit tax rate  $\tau_L$  reduces first-period labor supply. As argued above, the implicit tax rate depends, through the tax-benefit link, on the retirement date  $x$ . We now set  $R^P = 1$ , an assumption we employ in the rest of the paper, and use  $m - (1 - x)m' = m_0$  from (4) to obtain

$$\hat{\tau}_L = \frac{\tau m_0 x}{(1 - \tau_L) R} \cdot \hat{x}. \quad (10)$$

Consequently, intensive labor supply of young workers is linked to the retirement behavior—or extensive labor supply—of old agents, according to

$$L'(x) = \frac{dL}{d\tau_L} \cdot \frac{d\tau_L}{dx} = -\Psi < 0, \quad \Psi \equiv \frac{\sigma L}{1 - \tau_L} \cdot \frac{m_0 \tau}{R} > 0, \quad (11)$$

reflecting the fact that longer working life raises the effective tax rate on young workers.

## 2.3 Retirement Decision

It is assumed that continued employment leads to progressively increasing disutility of labor market participation of older workers. The retirement decision in (7) balances the marginal cost of labor market participation  $\beta\phi'(x)$  against the income differential between wages and pension earnings that becomes available by postponing retirement by another instant. The impact of the pension system on retirement behavior can be summarized by a single effective tax measure that is obtained upon rewriting (7) as

$$\beta\phi'(x) = (1 - \tau_R)W, \quad \tau_R \equiv \tau + \frac{P}{W} - \frac{1 - x}{W} \frac{\partial P}{\partial x}, \quad (12)$$

where  $\tau_R$  is a participation tax rate, often called the implicit retirement tax.

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<sup>4</sup>For a variable  $y$ ,  $\hat{y}$  represents the relative change  $\hat{y} \equiv dy/y$ . The change in the tax rate is relative to the tax factor,  $\hat{\tau} \equiv d\tau/(1 - \tau)$ .

It summarizes all fiscal incentives and disincentives for retirement in a single metric, which consists of: i) the wage taxes paid on a worker's salary, ii) the pension foregone with continued employment, and iii) the pension increase over the remaining retirement period if the system incorporates actuarial adjustment. To obtain the participation tax rate, all the costs and benefits are expressed as a percentage of a worker's gross wage. The "implicit retirement tax", so termed in the literature on pension economics, is entirely parallel to the participation tax analyzed in the literature on extensive labor supply by researchers such as Saez (2002), Immervoll et al. (2007), and Kleven and Kreiner (2006). Note, in particular, how an actuarial adjustment of pensions in the sense of Gruber and Wise, ( $\partial P/\partial x > 0$ ), lowers the effective retirement tax. This adjustment compensates for prolonged contribution payments due to continued work and a shorter retirement period and, hence, a shorter period of pension take-up. In a Beveridge type system without a tax-benefit link ( $m = 0$ ) and, thus, with a flat pension, the retirement tax would equal  $\tau_R = \tau + P/W$ , i.e. the sum of the contribution plus the replacement rate. Finally, the retirement tax is zero ( $\tau_R = 0$ ) in the fully funded system. In this case the pension is increased in an actuarially fair way when retirement is postponed, in order to compensate for the extra contributions and foregone pensions over the longer contribution period and the shorter duration of benefits.

To measure how retirement behavior responds to fiscal incentives, we calculate the log-derivative of (12),

$$\hat{x} = -\eta \cdot (\hat{\tau}_R + \hat{\beta}), \quad \eta \equiv \frac{\phi'}{x\phi''} > 0. \quad (13)$$

The parameter  $\eta$  expresses the elasticity of labor market participation. Participation declines and retirement occurs earlier when the effective tax rate  $\tau_R$  increases. A larger disutility  $\beta$  from continued work is meant to reflect exogenous socioeconomic factors leading to a trend to earlier retirement that will be explored in greater detail below.

Since the participation tax rate  $\tau_R$  is a function of  $x$ , it is important to explore its properties further. Since wages are fixed, we let  $P = pW$  and  $B = bW$ , and first rewrite

pension earnings in (3) as

$$p = m(x) \tau z(x) + b, \quad z(x) = L(x) + x, \quad (14)$$

where  $z$  determines the pension assessment base. The participation tax rate becomes

$$\tau_R \equiv \tau + p - (1 - x) p', \quad p' \equiv \partial p / \partial x. \quad (15)$$

With an earnings-linked pension formula such as (14), pension entitlements become sensitive to the retirement date via three channels: i) postponing retirement augments the pension assessment base by prolonging the active working period in old age, which translates into a higher pension depending on the conversion factor  $m$ ; ii) postponing retirement increases, however, (see (10)), the implicit tax rate on young workers, thereby discouraging intensive labor supply  $L$  and shrinking the assessment base, which leads to smaller pensions; and iii) the system could directly encourage postponed retirement by raising the conversion factor  $m$ . For convenience, we employ primes to denote the partial derivatives of  $m$ ,  $z$  and  $p$  with respect to  $x$ . The first two effects are summarized by  $z' > 0$ , which is positive if the intensive labor supply elasticity is not too large.<sup>5</sup> The last effect is  $m' \geq 0$ , and will be zero if the system provides no actuarial adjustment with respect to the retirement date. The sensitivity of pension size with respect to the chosen retirement date is thus

$$p' = \tau \cdot [zm' + mz'] > 0, \quad p'' = \tau \cdot [2z'm' + zm'' + mz'']. \quad (16)$$

We next analyze the effect of an extended working life on the participation tax. Differentiating (15) with respect to  $x$ , substituting (16), and using  $(1 - x)m'' = m'$  and  $m - (1 - x)m' = m_0$  from (4), we obtain

$$\frac{\partial \tau_R}{\partial x} \equiv \tau'_R = \tau \cdot [2m_0 z' - (1 - x)mz''] \geq 0, \quad (17)$$

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<sup>5</sup>To guarantee  $z' = 1 + L' > 0$ , we assume  $\Psi < 1$  (see equation (11) above), which holds for sufficiently small values of  $m_0$  and  $\sigma$ .

where  $z'' = L'' < 0$ .<sup>6</sup> Postponed retirement raises (resp. leaves unaffected) the participation tax. If there is no tax-benefit link, the participation tax rate is independent of the retirement date. If the conversion factor remains fixed and excludes any actuarial adjustment ( $m_0 > 0$  and  $\alpha = 0$ ), then  $z' > 0 > z''$ , implying a higher participation tax due to postponed retirement,  $\tau'_R > 0$ . If, instead, the conversion factor is actuarially adjusted to the retirement date ( $m = \alpha / (1 - x)$  and  $m_0 = 0$ ), the participation tax is also independent of the retirement date. In this case, with  $(1 - x)m = \alpha$ , retirement behavior does not influence the implicit tax on the young, so that first period labor supply remains unaffected and the assessment base satisfies  $z' = 1$  and  $z'' = 0$ .

## 2.4 Equilibrium

Our model is very stylized with only three overlapping generations and two periods. The focus is on generation 1 which is young in period 1 and old in period 2. To close the model, we assume the existence of an initial old generation of pensioners (generation 0) which coexists in period 1 with a young generation 1. We further assume a future generation of workers in period 2 which lives for one period and coexists with generation 1 when it is old. The upper index identifies generations 0 ‘old’ and  $f$  ‘future’, while variables without an upper index refer to the active generation 1, which is the only generation living over the entire two period life-cycle. The only activity of the old generation 0 is to consume PAYG pensions that must be paid from the contributions of generation 1

$$C^0 = P^0, \quad V^0 = C^0 / R. \quad (18)$$

Since our focus is on the behavior of generation 1, we assume away labor market participation on the part of generation 0. In other words, it is fully retired. The counterpart of generation 0 is a ‘future’ generation, which lives for only one period and inelastically supplies one efficiency unit of labor. In period 2, both the young and the old of generation 1 receive a competitive wage  $W = 1$ . Members of the future generation are assumed to

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<sup>6</sup>Observe that  $z''$  is negative. Given the assumption  $\sigma < 1$ , (10)–(11) imply  $z'' = L'' = -\frac{1-\sigma}{\sigma \cdot L} \cdot \Psi^2 < 0$ .

be fully employed. Their sole activity is to consume fixed labor earnings, after paying contributions to finance pensions of the then old generation 1. This reflects the fact that any PAYG pension system basically redistributes from future to present generations:

$$V^f = C^f = (1 - \tau)W. \quad (19)$$

The budgets of the PAYG system in periods 1 and 2 are

$$p^0 = \tau L, \quad (1 - x)p = \tau \cdot (1 + x). \quad (20)$$

We again employ the normalization  $P^0 = p^0W$  and  $P = pW$ . In the second period,  $\tau$  represents the contributions from the future generation and  $\tau x$  from the active part of the old of generation 1. Consequently, the pension is partly funded by an intergenerational transfer.<sup>7</sup> For the rest of the paper, we maintain  $W = 1$  and suppress  $W$ .

Given a Ricardian technology, output in period 1 is simply  $L$ . Substituting (20) into the budget identity (1) and using (18) yields the GDP identity  $L = C_1 + C^0 + S$  for the first period. Output is spent on consumption by young and old agents and on private investment  $S$ .<sup>8</sup> In the second period, new output  $1 + x$  is produced by generation 2 and by the still active part of generation 1. To obtain output market clearing, we aggregate (1) and (19) and substitute for (20) to yield:  $C_2 + C^f = 1 + x + RS$ . Second period GDP equals new output plus the yield on first period investment. Since the world ends thereafter, output is fully consumed.

## 2.5 Early Retirement

The equilibrium of the economy is fully characterized by a retirement age  $x$  and a “flat”, lump-sum pension  $b$  that simultaneously satisfy the extensive labor market condition (12)

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<sup>7</sup>In the funded system, the budget would apply to each person separately, making the generational account zero and eliminating intergenerational redistribution:  $(1 - x)p = \tau \cdot (LR + x)$ .

<sup>8</sup>The investment technology is linear with coefficient  $R$  and present and future consumption are perfect substitutes. Since it is not required for the present purposes, we intentionally leave savings and investment undetermined in our model. Alternatively, we could impose a small open economy assumption.

and the budget constraint (20).<sup>9</sup> The linearized versions of these two conditions, which take into account the intensive labor supply choice in (11), are derived in the appendix — see (A.2) and (A.4) — and are illustrated in the  $(x, b)$  plane by Figure 1. The retirement condition describes a downward-sloping relationship, since a higher flat pension makes early retirement more attractive, which reduces the retirement age. In contrast, the budget condition is upward-sloping, since the PAYG system can support a greater level of flat pensions over the remaining retirement period when the working life of agents is extended. The intersection of the two (linear) relationships determines the equilibrium values of  $x$  and  $b$ .

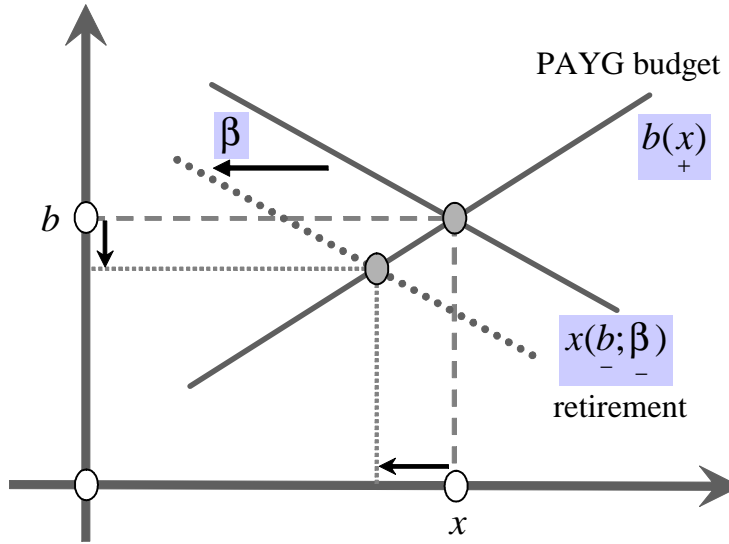


Fig. 1: Early Retirement

Before proceeding with an analysis of parametric pension reform, we first illustrate how an exogenous trend toward early retirement alters labor market choices on both margins and affects the pension system. An early retirement “trend” results from exogenous socioeconomic factors and is modeled by an increase in the preference parameter  $\beta$  that determines the disutility of old-age labor market participation. Holding the pension

<sup>9</sup>Our subsequent analysis refers, then, to a defined contribution system in which the contribution rate is fixed and pension size must ultimately be adjusted to guarantee the system’s solvency.

parameters fixed, equations (A.2) and (A.4) then simplify to

$$\hat{x} = -\frac{\eta}{1+\eta\varepsilon} \cdot \frac{db}{1-\tau_R} - \frac{\eta}{1+\eta\varepsilon} \cdot \hat{\beta}, \quad db = \frac{\tau_R x}{1-x} \cdot \hat{x}, \quad (21)$$

which we solve for the equilibrium responses:

$$\begin{aligned} \hat{x} &= -\frac{\eta}{1+\eta\varepsilon} \cdot \frac{1}{\nabla} \cdot \hat{\beta} < 0, \\ db &= -\frac{\tau_R x}{1-x} \cdot \frac{\eta}{1+\eta\varepsilon} \cdot \frac{1}{\nabla} \cdot \hat{\beta} < 0, \\ \nabla &\equiv 1 + \frac{\tau_R}{1-\tau_R} \cdot \frac{\eta}{1+\eta\varepsilon} \cdot \frac{x}{1-x} > 0. \end{aligned} \quad (22)$$

Not surprisingly, a preference shift toward early retirement reduces participation in the old-age labor market,  $\hat{x} < 0$ .

Furthermore, it requires budget consolidation to keep the system sustainable, and, consequently, leads to pension cuts,  $db < 0$ , as Figure 1 illustrates.<sup>10</sup> Interestingly, early retirement also reduces the implicit retirement tax rate in equilibrium,

$$\hat{\tau}_R = \varepsilon \cdot \hat{x} + \frac{db}{1-\tau_R} < 0. \quad (23)$$

The result is, again, quite intuitive. Not only does the participation tax decline when the flat portion  $b$  of the overall pension falls, it also declines with an earlier retirement date.

The latter effect occurs via  $\varepsilon \equiv \tau'_R x / (1 - \tau_R)$  and is present only if the earnings-linked part of pension earnings is relatively insensitive to variations in retirement behavior. In this case the conversion factor depends largely on the fixed term  $m_0$  and does not compensate sufficiently in terms of pension supplements  $p'$  received for the prolonged contribution and shorter retirement periods. This, in turn, magnifies the imbalance between the marginal returns and costs of postponing retirement, implying that the participation tax rate *increases* with the retirement date,  $\tau'_R > 0$ . Correspondingly, the participation tax rate

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<sup>10</sup>Observe, however, that an explicit consolidation is necessary only when the system is not actuarially fair in the sense of Gruber and Wise and features a positive  $\tau_R$ . An actuarially fair system with  $\tau_R = 0$  consolidates automatically, since earlier retirement reduces the conversion factor, reflecting the resulting longer retirement and shorter contribution periods.

*declines* when agents retire earlier. This reduction, of course, tends to encourage later retirement, but cannot offset the “trend” to early retirement from the original preference shock.

Irrespective of whether the system includes an actuarially fair adjustment for changes in the length of the retirement period, we find, interestingly, that early retirement raises intensive labor supply of younger workers. Using (9)–(11), we obtain

$$\hat{\tau}_L = \frac{\tau m_0 x}{(1 - \tau_L) R} \cdot \hat{x} < 0 \quad \Rightarrow \quad \hat{L} = -\sigma \cdot \hat{\tau}_L > 0. \quad (24)$$

The intuition for this result is best understood by reference to the Bismarckian system with a fixed conversion factor,  $m = m_0$ . In this case contribution payments yields pension gains earlier in life and over a longer retirement period when the retirement date is moved forward. Therefore, the implicit tax rate defined in (6) must fall, stimulating intensive labor supply. Moreover, even if the conversion factor  $m$  includes an actuarial component, the implicit tax rate on the young falls, as long as the reduction in the conversion factor is insufficiently great.<sup>11</sup>

## 3 Efficiency of Public Pensions

### 3.1 Welfare Measure

We need a consistent welfare metric to judge the efficiency of pension systems. To this end, we use the PAYG budgets in (20) to restate indirect utility of all three generations:

$$\begin{aligned} V^0 &= p^0/R = \tau L/R, \\ V &= (1 - \tau) L - \varphi(L) + [x(1 - \tau) + (1 - x)p - \beta\phi(x)]/R, \\ V^f &= (1 - \tau) = (1 - \tau) + \tau \cdot (1 + x) - (1 - x)p. \end{aligned} \quad (25)$$

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<sup>11</sup>The implicit tax rate on intensive labor supply is independent of retirement behavior only if the conversion factor depends exclusively on retirement duration, i.e.  $m_0 = 0$  and  $m = \alpha/(1 - x)$  imply a constant  $\tau_L = \tau(1 - \alpha/R)$ .



The utilitarian social welfare function, also employed by Calvo and Obstfeld (1988), is the discounted sum of individual utilities

$$\Phi = RV^0 + V + V^f/R = L - \varphi(L) + \frac{1}{R}[1 + x - \beta\phi(x)], \quad (26)$$

where the second equality follows upon substituting (20). This welfare function exclusively reflects economic efficiency and does not incorporate distributional concerns.<sup>12</sup>

Given that intensive and extensive labor supply are the only behavioral margins, the welfare effects of pension policy must be proportional to changes in  $x$  and  $L$ . Taking the differential of (26), substituting for the private choices of work effort and retirement in (6) and (12) and letting  $W = 1$ , we find

$$d\Phi = [1 - \varphi'(L)]dL + \frac{1 - \beta\phi'(x)}{R}dx = \tau_L \cdot dL + \frac{\tau_R}{R} \cdot dx. \quad (27)$$

Note that the coefficients on  $dL$  and  $dx$  for the change in welfare  $d\Phi$  reflect the differences between the social and private returns of a marginal increase in hours worked, 1 vs.  $1 - \tau_L$ , and in the retirement date, 1 vs.  $1 - \tau_R$ . Substituting for  $\hat{L}$  and  $\hat{x}$  from (9) and (13) (and holding  $\hat{\beta} = 0$ ), the welfare effects become

$$d\Phi = \tau_L L \cdot \hat{L} + \frac{\tau_R x}{R} \cdot \hat{x} = -\tau_L \cdot \sigma L \cdot \hat{\tau}_L - \tau_R \cdot \eta \frac{x}{R} \cdot \hat{\tau}_R. \quad (28)$$

The welfare impact of any behavioral changes induced by pension reform is, to the first order, proportional to the effective tax rates on work effort and old age participation. The pension system is the only source of inefficiency in our simple framework. If it were absent, allocation would be Pareto optimal. Introducing small contributions and pension entitlements would, to the first order, entail a zero marginal welfare impact.

### 3.2 Higher Statutory Tax Rate

To study the labor market impact and the efficiency effects of PAYG pensions, we first consider an increase in the statutory contribution rate  $\tau$ . Since the analysis of the general

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<sup>12</sup>This is less restrictive than it seems. As in Keuschnigg (1994), one could analytically separate efficiency from intergenerational redistribution. In Demmel and Keuschnigg (2000), this decomposition was used to construct an (ex ante) Pareto-improving reform.

case is quite complex, we concentrate on three specific scenarios to bring out the main message of our analysis. First, we consider complete actuarial fairness in the sense that the unfunded system adjusts the earnings-linked pension to take into account the length of the retirement period. This case emphasizes that while actuarial adjustment in the sense of Gruber and Wise eliminates the distortion in the retirement date, it is insufficient to ensure that the labor market is neutral with respect to the pension system. The second scenario assumes a fixed labor supply of younger workers and incomplete actuarial adjustment in the pension formula. Here, we show that a Bismarkian system with a fixed tax-benefit link mitigates, but does not remove, the distortion in the retirement decision. The third scenario entirely eliminates any tax-benefit link and considers the labor market impact of flat pensions unrelated to past earnings. The succeeding section will then characterize the excess burden of this case, where labor market is distorted both on the intensive and extensive margins.

**Actuarial Fairness:** A number of countries have reformed their earnings-linked PAYG system by including pension supplements in the sense of Gruber and Wise to compensate for postponed retirement. If the pension rule is made sufficiently sensitive to the choice of retirement date and adjusts the conversion factor in an actuarially fair way to reflect the longer contribution period and the shorter length of the remaining retirement period, all distortions with regard to labor market participation of older people can be eliminated. In our simple framework, this calls for a conversion factor in (4) equal to  $m(x) = 1/(1-x)$  with  $\alpha = 1$  and  $m_0 = 0$ . In this case,  $(1-x)m' = m$ . Since it implies  $\Psi = 0$ , we find from (B.5) in the appendix that the direct effect of the contribution rate, for any given retirement date  $x$ , on the participation tax rate is zero,  $\partial\tau_R/\partial\tau = 0$ . To understand why, one must note that the fair conversion factor  $(1-x)m = 1$  eliminates any sensitivity of the implicit tax rate  $\tau_L$  with respect to the retirement date so that intensive labor supply of younger workers becomes independent of the retirement decision. Consequently, the sensitivity of the assessment base  $z = L + x$  with respect to retirement reduces to the retirement margin only,  $z' = 1$  (which obviously leads to  $\partial z'/\partial\tau = 0$ ). The increase in the

assessment base  $z'$  on account of a longer contribution period, and any direct impact  $\partial z/\partial \tau$  of the first period labor supply response on the assessment base, are fully translated into an adjustment of the pension size so that the effective retirement tax is unaffected. Using in (B.3) the fact that a fair system is characterized by  $(1-x)m' = m$ ,  $(1-x)m = z' = 1$  and  $\partial z'/\partial \tau = 0$ , and substituting into (B.1), indeed proves  $\partial \tau_R/\partial \tau = 0$ .

However, this does not mean that such a system does not influence the retirement date. The level of the participation tax rate is positive as long as there is a flat, lump-sum pension,  $\tau_R = b$ . To see this, note the pension formula  $p = m\tau z + b$ , with  $p' = \tau[m'z + mz']$ . Using  $z' = 1$ ,  $(1-x)m' = m$  as well as  $(1-x)m = 1$  in (15) confirms the result. If the higher contribution rate raises extra revenues beyond what is needed to pay for the higher earnings-linked pensions, the flat pension  $b$  becomes more generous, which, in turn, raises the participation tax rate and leads to earlier retirement.

The extent of the tax revenue increase depends, of course, also on the resulting intensive labor supply response. Even if the system is actuarially fair with respect to the retirement date, the implicit tax rate on young workers is still positive,  $\tau_L = \tau \cdot (1 - 1/R) > 0$ , since an unfunded system does not pay interest on accumulated contributions. An increase in the statutory contribution rate thus raises the effective tax component on contributions and discourages intensive labor supply. To verify these statements, we solve the system stated in (A.2) and (A.4). Since  $z' = 1$  and  $m_0 = z'' = 0$  in the present scenario, we have  $\tau'_R = 0$  in (17), which eliminates the elasticity  $\varepsilon$  from the resulting expressions. Together with  $\partial \tau_R/\partial \tau = 0$ , the system reduces to

$$\hat{x} = -\frac{\eta}{1 - \tau_R} \cdot db, \quad db = \frac{\tau_R x}{1 - x} \cdot \hat{x} + \left[ \frac{b}{\tau} + \frac{\tau_L}{1 - \tau_L} \sigma m L \right] \cdot d\tau, \quad (29)$$

where the terms in square brackets replaces the one in (A.4). To see this, note that the PAYG budget constraint in (20) and the pension formula imply  $\frac{1+x}{1-x} = p/\tau = mz + b/\tau$ . Using this expression and combining with (B.2)–(B.3) yields the term in square brackets in (29).

The resulting solution is illustrated as in Figure 1. The budget line shifts up in response to the rise in  $\tau$ , while the position of the retirement locus remains unchanged.

Consequently, agents retire earlier, and the system affords a more generous flat pension component. The comparative static solution, using (29), corresponds to

$$\begin{aligned}\hat{x} &= -\frac{\eta}{1-\tau_R} \frac{1}{\nabla} \left[ \frac{b}{\tau} + \frac{\tau_L}{1-\tau_L} \sigma m L \right] \cdot d\tau < 0, \\ db &= \frac{1}{\nabla} \left[ \frac{b}{\tau} + \frac{\tau_L}{1-\tau_L} \sigma m L \right] \cdot d\tau > 0, \\ \nabla &= 1 + \frac{\tau_R}{1-\tau_R} \frac{x}{1-x} \eta.\end{aligned}\tag{30}$$

We have thus seen that expanding the system with an actuarially fair adjustment of the conversion factor not only pays for a more generous earnings-linked pension, but also for a higher flat pension. The latter effect raises the participation tax rate and results in early retirement. In addition, the implicit tax rate on the young  $\tau_L = \tau \cdot (1 - 1/R)$  increases, because the adjustment of the conversion factor cannot undo the fact that contributions in an unfunded system pay no interest and, thus, partly represent a tax on the young that distorts intensive labor supply,  $\hat{L} = -\sigma \cdot \hat{\tau}_L < 0$ . By (28), aggregate welfare declines on both margins. The welfare loss would be zero on the extensive retirement margin if, in the initial equilibrium, the flat pension and, thus, the participation tax rate were zero:  $\tau_R = b = 0$ .

**Fixed Labor Supply of Young Workers:** When labor supply is completely insensitive to variations in effective wages ( $\sigma = 0$ ), the pension assessment base  $z = L + x$  depends only on changes in the retirement date ( $z' = 1$ ), so that  $\partial z / \partial \tau = \partial z' / \partial \tau = 0$ . In evaluating the impact of the statutory contribution rate on the participation tax rate, we find from (B.1)–(B.5)

$$\partial \tau_R / \partial \tau = 1 - \alpha + m_0 [z - (1 - x)] \geq 0.\tag{31}$$

We assume in this scenario that the conversion factor  $m$  is ‘imperfectly’ fair—as it in fact is in most countries—and allow for arbitrary parameter values  $\alpha \in [0, 1]$  and  $m_0$ .<sup>13</sup>

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<sup>13</sup>With  $z' = 1$ , (15) and (16) imply  $\tau_R = b + \tau [1 - \alpha + m_0 (z - (1 - x))]$ . The second term shows how the earnings-linked pension leads to a positive participation tax rate. If it were positive and, thus, unfair initially, then the participation tax will increase with a higher contribution rate.

If the conversion factor were fair,  $\alpha = 1$  and  $m_0 = 0$ , a higher contribution rate would not affect the participation tax rate.

We now solve for the equilibrium impact of the policy change. With fixed labor supply,  $\partial p / \partial \tau = mz$ . The PAYG budget constraint (20) implies  $(1 + x) / (1 - x) = p / \tau$  while the pension formula is rearranged to yield  $mz = (p - b) / \tau$ . Substituting this expression into the term square brackets in (A.4), the equilibrium system (A.2) and (A.4) simplifies to  $\hat{x} = -\frac{\eta}{1+\eta\varepsilon} \frac{1}{1-\tau_R} [db + \frac{\partial \tau_R}{\partial \tau} d\tau]$  and  $db = \frac{\tau_R x}{1-x} \cdot \hat{x} + \frac{b}{\tau} \cdot d\tau$ . Noting the definition of  $\nabla > 0$  in (22), the corresponding solution is

$$\begin{aligned}\hat{x} &= -\frac{1}{1-\tau_R} \frac{\eta}{1+\eta\varepsilon} \frac{1}{\nabla} \left( \frac{b}{\tau} + \frac{\partial \tau_R}{\partial \tau} \right) \cdot d\tau < 0, \\ db &= -\frac{1}{\nabla} \left[ \frac{\tau_R}{1-\tau_R} \frac{x}{1-x} \frac{\eta}{1+\eta\varepsilon} \frac{\partial \tau_R}{\partial \tau} - \frac{b}{\tau} \right] d\tau.\end{aligned}\tag{32}$$

The interpretation is of (32) straightforward. If the system is unfair with respect to the length of remaining retirement, as in the standard Bismarckian system with a fixed tax-benefit link  $m_0$ , the agent *loses* when retiring an instant later. The net effect of the extra contribution plus pension foregone minus the present value of the increase in future pensions reflects a positive participation tax. The loss on the extensive margin induces agents to retire earlier, thereby worsening the system's budgetary position. Consequently, the retirement date declines and the flat pension is reduced to keep the system sustainable (if  $b$  is not too large initially). As a check on consistency, a fair system would involve  $p = m\tau z$  with  $b = 0$  and  $m = 1 / (1 - x)$ , implying  $\partial \tau_R / \partial \tau = 0$ , as argued above. There would then be no effect on the retirement date.<sup>14</sup> Given the impact on retirement, the implication for economic efficiency in (28) is also clear. With a positive participation tax, retirement already occurs inefficiently early, so that an expansion of the system can only reinforce this distortion and lead to further efficiency losses.

**Flat Pensions:** Labor market distortions are at their highest, if pensions are lump-sum from an individual's perspective and completely unrelated to past earnings. The absence of a tax-benefit link is given by  $\alpha = m_0 = m = 0$ , reducing the pension formula to

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<sup>14</sup>The system would still redistribute intergenerationally, an issue that we do not analyze here.

$p = b$ . The effective tax rates on the intensive labor supply of younger workers and on the participation of their older counterparts are  $\tau_L = \tau$  and  $\tau_R = \tau + p$ , respectively. Clearly, the participation tax rate is independent of the retirement date, implying  $\tau'_R = \varepsilon = 0$ . The absence of a tax-benefit link also implies  $\partial p / \partial \tau = 0$  and, of course,  $\partial \tau_R / \partial \tau = 1$ . In this case, the system in (A.2) and (A.4) reduces to  $\hat{x} = -\frac{\eta}{1-\tau_R} [db + d\tau]$  and  $db = \frac{\tau_R x}{1-x} \cdot \hat{x} + \frac{1+x}{1-x} \cdot d\tau$ , yielding a solution

$$\begin{aligned}\hat{x} &= -\eta \cdot \hat{\tau}_R = -\eta \cdot \left[ \frac{1+x}{1-x} + 1 \right] \frac{1}{\nabla} \frac{d\tau}{1-\tau_R} < 0, \\ db &= \left[ \frac{1+x}{1-x} - \frac{\tau_R}{1-\tau_R} \frac{x}{1-x} \eta \right] \frac{1}{\nabla} d\tau > 0, \\ \nabla &= 1 + \frac{\tau_R}{1-\tau_R} \frac{x}{1-x} \eta.\end{aligned}\tag{33}$$

An increased contribution rate in a system without tax-benefit link leads to earlier retirement and more generous flat pensions. The pension level grows less than proportionally, because earlier retirement erodes the tax base, depending on the magnitude of the participation distortion  $\tau_R$  and the extensive elasticity  $\eta$ . The increase in the effective tax rate  $\tau_L = \tau$  also reduces first period labor supply and the welfare of young workers.

### 3.3 Excess Burden

This subsection provides a sharper characterization of the efficiency loss from expanding a PAYG pension system without a tax-benefit link. The absence of a tax-benefit link and the assumption of intertemporally separable preferences imply that pension budgets and labor market behavior can be analyzed independently in each period without any spillover. Although special, this case allows for a particularly simple and illuminating characterization of the excess burden from lump-sum PAYG pensions. Intensive labor supply  $L$  occurs in the first period and depends only on the first period tax rate  $\tau_1$ , while retirement behavior refers to the second period and depends exclusively on the second period tax rate  $\tau_2$ . In this case,  $\tau_L = \tau_1$  leads to an intensive labor supply response in the first period equal to  $\hat{L} = -\sigma \cdot \hat{\tau}_1$ . Substituting this together with (33) into (28) yields

$$d\Phi = -\frac{\tau_L}{1-\tau_L} \sigma \cdot L d\tau_1 - \frac{\tau_R}{1-\tau_R} \eta \cdot \frac{x}{1-x} \frac{2}{\nabla R} d\tau_2.\tag{34}$$

Clearly, a permanent increase in contribution financed flat pensions ( $d\tau_1 = d\tau_2$ ) reduces aggregate welfare on both the intensive and extensive margins of labor supply.

We now develop a metric to evaluate the marginal excess burden of a tax, which is defined as the marginal loss in welfare in percent of net tax revenue raised at the margin. Using the budget relationships in (20) for a flat pension system, we write the intertemporal budget constraint as

$$T \equiv \tau_1 L + \frac{(\tau_2 + p) \cdot x}{R} = p^0 + \frac{p - \tau_2}{R}. \quad (35)$$

In measuring the excess burden of a PAYG system, we must take care of the overall impact of the behavioral response on the public budget. Not only the tax  $\tau_2$  but also the spending  $p$  distorts labor market participation of older workers. A policy-induced trend to early retirement erodes the contribution tax base and also generates extra pension claims. For this reason, the change in contribution revenues would capture only a part, perhaps relatively unimportant, of the overall fiscal cost of early retirement. We thus need to consider the participation tax revenue in the second period, equal to  $(\tau_2 + p)x = \tau_R x$ . It measures the total gain in the public budget when labor market participation is increased from zero to  $x$  and consists of contribution payments plus expenditure savings on pensions. The meaning of this definition is also seen from the budget constraint in (1),  $C_2 = RS + x + p - \tau_R x$ . If there were no participation at all, pension spending would have been  $p$ . When retirement is postponed by  $x$ , the individual pays extra contributions and foregoes pensions over this time interval, which adds up to a total loss  $\tau_R x$ . The public budget improves by the same amount. This “participation tax revenue”  $(\tau_2 + p)x = p - \tau_2 x$  is equal to maximum pension spending  $p$ , reduced by the contribution  $\tau_2$  from the future generation.

With lump-sum pensions,  $\tau_R = \tau_2 + p$  and  $\tau_L = \tau_1$ . Using the retirement response to an increase in contribution-financed flat pensions in (33), as well as  $\hat{x} = -\eta \hat{\tau}_R$ , yields the total impact on the present value of PAYG budget

$$dT = \left[ 1 - \frac{\tau_L}{1 - \tau_L} \sigma \right] \cdot L d\tau_1 + \left[ 1 - \frac{\tau_R}{1 - \tau_R} \eta \right] \cdot \frac{x}{1 - x} \frac{2}{\nabla R} d\tau_2. \quad (36)$$

According to (36), the present value of the budget impact depends on the size of the induced labor supply response on both the intensive and extensive margins.

The marginal excess burden is defined as the marginal, income equivalent welfare loss per additional unit of net tax revenue raised, expressed in present value over all periods. Using (34) and (36)

$$\Gamma \equiv -\frac{d\Phi}{dT} = \frac{\frac{\tau_L}{1-\tau_L}\sigma \cdot \omega_L + \frac{\tau_R}{1-\tau_R}\eta \cdot \omega_x}{1 - \frac{\tau_L}{1-\tau_L}\sigma \cdot \omega_L - \frac{\tau_R}{1-\tau_R}\eta \cdot \omega_x}, \quad (37)$$

where weights  $\omega_L \equiv L / [L + \frac{x}{1-x} \frac{2}{\nabla R}]$  and  $\omega_x \equiv \frac{x}{1-x} \frac{2}{\nabla R} / [L + \frac{x}{1-x} \frac{2}{\nabla R}]$  indicate the relative importance of the intensive and extensive margins, such that  $\omega_L + \omega_x = 1$ . Moreover, the marginal cost of public funds is one plus the marginal excess burden

$$MCPF = 1 + \Gamma = \frac{1}{1 - \frac{\tau_L}{1-\tau_L}\sigma \cdot \omega_L - \frac{\tau_R}{1-\tau_R}\eta \cdot \omega_x}. \quad (38)$$

These are familiar formulas in the tax literature. In raising the contribution rate to pay for a pension rise, this policy causes people to choose early retirement. Each unit of earlier retirement causes a double burden on the fiscal budget equal to the participation tax rate. The general structure of the MCPF formula in (38) is parallel to that found in Kleven and Kreiner (2006), who also considered the welfare consequences of tax and benefit changes in a static model, and Immervoll et al. (2007). Their analyses is applied here with appropriate modifications to characterize the excess burden of public pensions. The excess burden with respect to the retirement decision is driven by the measures of the participation tax rate, or implicit retirement tax, as suggested by Gruber and Wise (1999b, 2005). The relevant retirement elasticity for Germany is estimated by Börsch Supan (2000).



## 4 Parametric Pension Reform

### 4.1 Stronger Tax-Benefit Link

Many countries recently reformed their PAYG pension systems. To undo some of their damaging labor market effects and, in particular, to raise the average retirement age, policy makers have aimed primarily at strengthening the tax-benefit link and introducing a greater degree of actuarial fairness. For example, in order to strengthen old age labor market participation, Austria has introduced substantial supplements to regular pensions when work is continued beyond the statutory retirement age and pension discounts, or ‘penalties’, for early retirement. Further, the length of the calculation period has been significantly prolonged: in other words, the number of years of past earnings that count towards future pensions has been increased. In addition, the pension system was harmonized so that some occupational groups, such as civil servants who previously received pensions largely unrelated to past earnings, have been integrated into the same earnings-linked system. These measures represent different ways of strengthening the tax-benefit link by making it more widespread, thereby reducing the importance of flat lump-sum pensions.<sup>15</sup>

Within our simple framework, we can analyze this policy initiative by considering an increase in the fixed component  $m_0$  of the conversion factor  $m = \alpha / (1 - x) + m_0$ . To avoid complex calculations that yield no additional insight, we set  $m_0 = 0$  in the initial equilibrium and allow  $\alpha \in [0, 1]$ . Since this clearly raises earnings-linked pension levels, we endogenously cut the lump-sum pension component  $b$  to satisfy the PAYG budget constraint when the statutory contribution rate is kept constant. Appendix B, see (B.6)–(B.10), computes the partial effects on the size of the earnings-linked pension and the participation tax rate. Among other results, we find that an increased conversion factor directly raises the pension level. It also lowers the effective tax rate of young workers, because they individually expect larger future pensions when working more.

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<sup>15</sup>See Knell et al. (2006) for an informative description of pension reform in Austria.

This stimulates labor supply, augments the assessment base, and further raises pension size. However, a larger pension raises the participation tax rate. On the other hand, this incentive for early retirement is mitigated by the fact that the policy measure also raises the pension supplement  $p$  that becomes available upon choosing a marginally higher retirement age. It must be kept in mind, nevertheless, that the flat pension is endogenously cut to sustain the PAYG budget, which, in turn, causes people retire later. To verify our logic, we solve the system (A.2) and (A.4) and note that  $\tau'_R = \varepsilon = 0$ , starting from a position of  $m_0 = 0$

$$\begin{aligned}\hat{x} &= \eta \cdot \left[ \frac{\partial p}{\partial m_0} - \frac{\partial \tau_R}{\partial m_0} \right] \frac{1}{\nabla} \frac{dm_0}{1-\tau_R} > 0, \\ db &= - \left[ \frac{\tau_R}{1-\tau_R} \frac{x}{1-x} \eta \frac{\partial \tau_R}{\partial m_0} + \frac{\partial p}{\partial m_0} \right] \frac{1}{\nabla} dm_0 < 0,\end{aligned}\tag{39}$$

where  $\nabla$  is given in (22). The sign of the comparative static effects is determining by evaluating the terms defined in (B.7)–(B.9), which yields

$$\frac{\partial p}{\partial m_0} - \frac{\partial \tau_R}{\partial m_0} = \tau \left[ (1-x) + \frac{\tau - \tau_L}{1 - \tau_L} \cdot \sigma L \right] > 0.\tag{40}$$

Hence, a tighter tax-benefit link raises the retirement age,  $\hat{x} > 0$ , and reduces the lump-sum pension level,  $db < 0$ . In addition, the partial derivatives in (B.7)–(B.10) imply  $\partial \tau_R / \partial m_0 > 0$  and  $\partial p / \partial m_0 > 0$ . Moreover, the lump-sum pension component falls to such an extent that in equilibrium, despite of the direct effect  $\partial \tau_R / \partial m_0 > 0$ , the participation

tax rate *declines*, which increases  $x$ . The solution is illustrated in Figure 2.

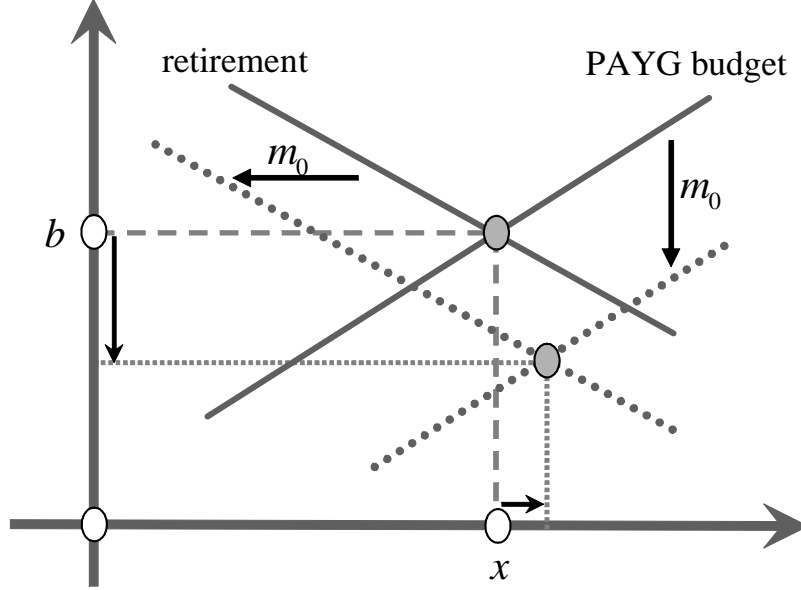


Fig. 2: Tighter Tax Benefit Link

As indicated, although the partial effect on the participation tax rate in (B.10) is positive, it falls in equilibrium due to the large reduction in lump-sum pensions, which results in a later retirement date. Noting the pension formula (14) and taking the differential of (15), with  $\varepsilon = 0$  due to  $m_0 = 0$  initially, yields equilibrium response of the participation tax

$$\hat{\tau}_R = \frac{\partial p}{\partial m_0} \frac{dm_0}{1 - \tau_R} + \frac{db}{1 - \tau_R} - (1 - x) \frac{\partial p'}{\partial m_0} \frac{dm_0}{1 - \tau_R} < 0. \quad (41)$$

Substituting the equilibrium changes of retirement age and lump-sum pensions as noted in (39) and using the partial effects stated in (40) and Appendix B, we find, after some lengthy computations,  $\hat{x} = -\eta \cdot \hat{\tau}_R > 0$ , with  $\hat{x} > 0$  as in (39). This reflects that fact that all retirement incentives are summarized in the participation tax rate.

The intensive labor supply response of young workers,  $\hat{L} = -\sigma \cdot \hat{\tau}_L$ , depends on the equilibrium change of the implicit tax rate  $\tau_L = \tau [1 - (1 - x) m/R]$ . Since the statutory

contribution rate remains constant, the log-differential yields

$$\hat{\tau}_L = -\frac{(1-x)\tau/R}{1-\tau_L} \cdot dm_0, \quad (42)$$

which implies that the tax-benefit link reduces the implicit tax rate on young workers, thereby stimulating intensive labor supply. Under the conditions stated above, a stronger tax-benefit link reduces the effective tax rates on both margins of aggregate labor supply, leading to (potentially) substantial welfare gains according to (28).

## 4.2 Greater Actuarial Fairness

We next explore the benefits of introducing a greater degree of actuarial fairness. Specifically, we first consider the effects of strengthening the tax-benefit link by raising the conversion factor so that pension earnings are more sensitive to the retirement date. The scenario, thus, involves an increase in the parameter  $\alpha$ , when the conversion factor is  $m = \alpha/(1-x)$ , with  $m_0 = 0$ . The lump-sum pension must be cut to keep the system sustainable when past earnings translate into more generous pensions. The appendix calculates in (B.11)–(B.14), for any given retirement date  $x$ , the partial effects and finds that the participation tax rate is reduced by<sup>16</sup>  $\partial\tau_R/\partial\alpha = -\tau$ , while the earnings-linked pension component becomes larger,  $\partial p/\partial\alpha > 0$ . Solving (A.2) and (A.4) yields<sup>17</sup>

$$\begin{aligned} \hat{x} &= \eta \cdot \frac{\tau + \partial p/\partial\alpha}{\nabla} \cdot \frac{d\alpha}{1-\tau_R} > 0, \\ db &= -\left[\left(1 + \frac{\tau - \tau_L}{1-\tau_L}\sigma\right)L + \left(1 - \frac{\tau_R}{1-\tau_R}\eta\right)x\right] \frac{\tau}{(1-x)\nabla} \cdot d\alpha, \end{aligned} \quad (43)$$

which imply an increase in the retirement date,  $\hat{x} > 0$ . Except for extreme cases, the lump-sum pension must be cut,  $db < 0$ , when the earnings-linked component becomes

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<sup>16</sup>In the specific case considered here, we can in fact get a closed form solution: since  $z' = 1$ , we have  $p' = \tau[m + m'z]$ . Using  $\tau_R = \tau + p - (1-x)p'$  and  $(1-x)m' = m$  yields  $\tau_R = b + (1-\alpha)\tau$ .

<sup>17</sup>If the coefficient  $m_0 = 0$  so that  $(1-x)m' = m$ , the following restrictions can be used:  $z' = 1$  and  $\Psi = 0 = z''$ , hence  $\tau'_R = \varepsilon = 0$ , as well as  $\partial\tau_R/\partial\alpha = -\tau$ . From (B.13),  $(1-x)\frac{\partial p'}{\partial\alpha} = \tau + \tau\left[\frac{z}{1-x} + m\frac{\partial z}{\partial\alpha}\right] = \tau + \frac{\partial p}{\partial\alpha}$ , where  $\frac{\partial p}{\partial\alpha} = \frac{\tau}{1-x}\left(z + \frac{\tau - \tau_L}{1-\tau_L}\sigma L\right)$  and  $\tau - \tau_L = \alpha\tau/R$ .

larger.<sup>18</sup> Moreover, the policy change is strictly welfare improving. Since  $\varepsilon = 0$ , the participation tax rate changes by  $\hat{\tau}_R = \frac{\partial p}{\partial \alpha} \frac{d\alpha}{1-\tau_R} + \frac{db}{1-\tau_R} - (1-x) \frac{\partial p'}{\partial \alpha} \frac{d\alpha}{1-\tau_R}$ . As before, substituting the solutions from (43) yields, after some manipulations, the result satisfying  $\hat{x} = -\eta \cdot \hat{\tau}_R$ . The rise in  $\alpha$  also lead to a decline in the implicit tax rate on younger workers. The results with respect to the effective tax rates is summarized as follows

$$\hat{\tau}_R = -\frac{\tau + \partial p / \partial \alpha}{\nabla} \frac{d\alpha}{1-\tau_R} < 0, \quad \hat{\tau}_L = -\frac{\tau}{R} \frac{d\alpha}{1-\tau_L} < 0. \quad (44)$$

Since both effective tax rates fall, aggregate labor supply on the intensive and extensive margins is stimulated. Depending on the magnitude of the initial labor market distortions, aggregate efficiency improves.

The scenario discussed above not only introduces more actuarial fairness, but also makes earnings-linked pensions more generous, since it raises the conversion factor. To a large extent, however, recent pension reform policy is dictated by the need to restore fiscal sustainability, a goal hardly compatible with replacing a greater part of past earnings. To be closer to actual policy challenges, we evaluate the following reform scenario: *raise* the parameter  $\alpha$  to introduce more actuarial fairness and at the same time *cut* the coefficient  $m_0$  to prevent pensions from becoming more generous:

$$dm_0 = -\frac{d\alpha}{1-x} \quad \Rightarrow \quad dm = \frac{m}{1-x} \cdot dx. \quad (45)$$

The scenario implies that the conversion factor  $m = \alpha / (1-x) + m_0$  remains constant for any given retirement behavior. The conversion factor increases only if the policy measure leads workers to postpone retirement. To keep calculations simple, we start from an initial situation of  $m_0 = 0$  so that  $m' = m / (1-x)$ .<sup>19</sup>

To derive the comparative static effects and the welfare consequences of this policy experiment, we need to determine the partial effects on pensions  $p$ , the participation tax rate  $\tau_R$  and the pension supplement  $p'$ . To do so, we impose the policy change  $dm_0 = -\frac{d\alpha}{1-x}$

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<sup>18</sup>A limited countervailing effect arises, since the pension is paid over a shorter period, which allows the possibility of a larger pension, when retirement is postponed.

<sup>19</sup>Strictly speaking,  $m_0 < 0$  after the policy change, to offset the increase in  $m$  due to a higher  $\alpha$ .

and evaluate derivatives at the initial position  $m_0 = 0$  and  $m = \alpha / (1 - x)$ . Using (B.7)–(B.8) and (B.12)–(B.13), as well as  $(1 - x) m \tau / R = \tau - \tau_L$  from the definition of the effective tax rate, shows that the partial effects on pension earnings completely cancel. The result is due to the fact that the policy initiative, for a given retirement date, holds the conversion factor constant

$$\begin{aligned} \frac{\partial p}{\partial \alpha} d\alpha + \frac{\partial p}{\partial m_0} dm_0 &= \left[ (1 - x) \frac{\partial p}{\partial \alpha} - \frac{\partial p}{\partial m_0} \right] \frac{d\alpha}{1 - x} = 0, \\ \frac{\partial \tau_R}{\partial \alpha} d\alpha + \frac{\partial \tau_R}{\partial m_0} dm_0 &= \left[ (1 - x) \frac{\partial \tau_R}{\partial \alpha} - \frac{\partial \tau_R}{\partial m_0} \right] \frac{d\alpha}{1 - x} = -\tau z \frac{d\alpha}{1 - x} < 0, \\ \frac{\partial p'}{\partial \alpha} d\alpha + \frac{\partial p'}{\partial m_0} dm_0 &= \left[ (1 - x) \frac{\partial p'}{\partial \alpha} - \frac{\partial p'}{\partial m_0} \right] \frac{d\alpha}{1 - x} = \frac{\tau z}{1 - x} \frac{d\alpha}{1 - x} > 0. \end{aligned} \quad (46)$$

The partial effect on the participation tax rate follows upon substituting (B.10) and (B.14) and is negative: greater actuarial fairness is designed to reduce the participation tax rate and to encourage workers to postpone retirement. To achieve this, the government must increase the pension supplement  $p'$  that becomes available for each instant of postponed retirement.

The equilibrium impact of the policy reform is found, as before, by solving the system (A.2) and (A.4). Using the results given above and noting  $\tau'_R = \varepsilon = 0$  if evaluated at  $m_0 = 0$ , we calculate

$$\hat{x} = \eta \cdot \frac{1}{1 - \tau_R} \frac{\tau z}{\nabla} \frac{d\alpha}{1 - x}, \quad db = \eta \cdot \frac{\tau_R}{1 - \tau_R} \frac{x}{1 - x} \frac{\tau z}{\nabla} \frac{d\alpha}{1 - x}, \quad (47)$$

where  $\nabla = 1 + \frac{\tau_R}{1 - \tau_R} \frac{x}{1 - x} \eta$ . As indicated, the policy experiment in (45) keeps pension size fixed if retirement date does not change, but offers larger pension supplements when retirement is postponed. Consequently, it succeeds in reducing the participation tax rate and encouraging later retirement. The scenario unambiguously raises the lump-sum pension  $b$  since it expands the assessment base and shortens the retirement period.

In equilibrium, with  $\varepsilon = 0$ , the effect of retirement choice  $x$  on  $\tau_R$  disappears. Substitution of (46) shows that the participation tax rate falls by

$$\hat{\tau}_R = -\frac{\tau z}{(1 - \tau_R) \nabla} \frac{d\alpha}{1 - x} < 0, \quad (48)$$

which confirms  $\hat{x} = -\eta \cdot \hat{\tau}_R$  and is consistent with (47). A welfare evaluation employing (28) requires the calculation of the effect on the effective tax rate on young workers

and their intensive labor supply response. Imposing the policy change noted above and calculating the differential of the implicit tax rate  $\tau_L = \tau [1 - (1 - x) m/R]$  at  $m_0 = 0$  yields

$$d\tau_L = \frac{\tau}{R} \cdot [mdx - (1 - x) dm] = 0. \quad (49)$$

According to (49), the effective tax rate on young workers is independent of the policy scenario in (45), implying that period labor supply remains constant. The experiment fails to reduce distortions faced by young workers and, thus, cannot promise any further efficiency gains on that margin. The main advantage of the policy package is the reduction of the participation tax rate. By encouraging later retirement, it potentially results in welfare gains on the extensive margin.

## 5 Conclusion

The potential labor market impact of pension reform is a prime policy concern. Aging and the socioeconomic trend to early retirement not only impose financial stress on the system, but are also an important factor in restraining aggregate employment. The need to provide incentives for the continuing labor market participation of older workers has, thus, received increasing attention among policy makers. For example, the tax character and the potentially harmful impact on labor supply incentives of prime-age workers is a particular concern. In this context, recent reform initiatives in many countries aim at reducing the large participation tax rates incorporated in current pension systems. For instance, pension formulas have been modified to offer income supplements for each year of postponed retirement and pension ‘penalties’ have been imposed when earlier retirement is chosen. Other measures seek to improve work incentives of younger, prime-age workers by strengthening the tax-benefit link. In Austria concrete examples of pension reforms include the “harmonization” of the pension system, with the consequence that civil servants and other employee groups who have previously received lump-sum pensions unrelated to past earnings, are now included in the same earnings-linked pension system.

Austria, along with other countries, has also lengthened the calculation period for the pension assessment base so that not only the best five years, but also the entire earnings history count in determining the size of the pension. These purpose of these reforms is to raise the share of prime-age workers who are subject to a tax-benefit link and will, as a result, perceive that their pension contributions have a lower tax component. As such, these reforms are suitable to stimulate labor supply and employment among younger workers.

This paper has proposed a simple model that captures the important interaction between labor supply incentives of prime-age workers and incentives for labor market participation of workers near retirement. We show that the joint policy goals of stimulating young and old age labor supply can conflict with each other. In a system with a tax-benefit link, raising the retirement age tends to raise the effective tax faced by young, prime-age workers. When the retirement date is postponed, the extra pension benefits expected by a young worker from increased earnings are obtained only in the more distant future and over a shorter retirement period. Consequently, these future earnings are discounted more heavily, which raises the tax component for any given pension contribution. For the same reasons, we find that an exogenous, socioeconomic trend to early retirement raises prime-age labor supply, which tends to offset the reduction in aggregate employment due to lower old age labor market participation. In view of this trade-off, policy makers should be careful to design reforms in a way that strengthens both margins of labor supply in an aging society.

Fortunately, our analysis shows that some recent reform approaches can attain this objective. If it is possible to cut lump-sum pensions, for example, by “harmonizing” the system, an increase in the tax-benefit link indeed tends to stimulate both margins of labor supply, regardless of whether the link is also made actuarially fair with respect to the retirement date. However, if the conversion factor determining pension size conditional on past earnings is made more sensitive with respect to retirement age *without* raising its overall magnitude, then such a reform, while encouraging old age labor market par-



ticipation, does not stimulate employment among prime-age workers. Nevertheless, this scenario shows that any given increase in the tax-benefit link is much preferred if it is also made actuarially fair in the sense of Gruber and Wise, compared to one that is not sensitive to a worker's retirement choice.

## Appendix

### A Comparative Statics

This appendix computes comparative static results. We log-linearize the model and compute proportional rates of change relative to a given initial equilibrium. Intensive labor supply in (11) depends exclusively on pension parameters and the retirement date. Taking account of this, equilibrium is given by a retirement date  $x$  and a flat pension  $b$  that satisfy the optimality condition for retirement (12) subject to (14) and budget balance of the PAYG system (20).

Pension earnings given by (14) are a complex function of the parameters of the system:  $p(x, b; \tau, m_0, \alpha) = m(x; m_0, \alpha) \tau z(x; \tau, m_0, \alpha) + b$ . Obviously,  $p' \equiv \partial p / \partial x$  is independent of the flat pension  $b$ . We derive how the relative change  $\hat{\tau}_R \equiv d\tau_R / (1 - \tau_R)$  of the participation tax rate depends on changes in retirement behavior,  $x$ , and pension parameters  $\tau, m_0, \alpha$  and  $b$ . The effective tax rate  $\tau_R \equiv \tau + p - (1 - x)p'$  is defined in (15). Define the elasticity  $\varepsilon \equiv \tau'_R x / (1 - \tau_R)$  where  $\tau'_R$  is given in (17), and note that pension parameters affect the participation tax rate by their impact on  $p$  and  $p'$

$$\hat{\tau}_R = \varepsilon \cdot \hat{x} + \frac{db}{1 - \tau_R} + \frac{\partial \tau_R}{\partial \tau} \frac{d\tau}{1 - \tau_R} + \frac{\partial \tau_R}{\partial m_0} \frac{dm_0}{1 - \tau_R} + \frac{\partial \tau_R}{\partial \alpha} \frac{d\alpha}{1 - \tau_R}. \quad (\text{A.1})$$

The derivatives of  $\tau_R$  will be specified later when we discuss specific policy scenarios. Substituting (A.1) into the retirement response noted in (13), we obtain, after rearranging, the following equation for the impact on retirement in terms of parametric shifts and the

change  $db$  in the endogenous level of flat pensions:

$$\hat{x} = -\frac{\eta}{1+\eta\varepsilon} \frac{1}{1-\tau_R} \left[ db + \frac{\partial\tau_R}{\partial\tau} d\tau + \frac{\partial\tau_R}{\partial m_0} dm_0 + \frac{\partial\tau_R}{\partial\alpha} d\alpha + (1-\tau_R) \hat{\beta} \right]. \quad (\text{A.2})$$

This equation corresponds to the retirement locus in Figures 1 and 2. It is downward sloping since a more generous flat pension induces, holding  $(\tau, m_0, \alpha)$  constant, earlier retirement.

The other constraint to pin down equilibrium is the condition for budget balance in (20):  $\tau \cdot (1+x) = (1-x)p$ . Taking the differential of revenues and pension spending, we obtain

$$(1+x)d\tau + \tau dx = (1-x) \left[ p' dx + \frac{\partial p}{\partial\tau} d\tau + \frac{\partial p}{\partial m_0} dm_0 + \frac{\partial p}{\partial\alpha} d\alpha + db \right] - p dx. \quad (\text{A.3})$$

Using the fact that  $\tau_R = \tau + p - (1-x)p'$ , we solve for  $db$  in terms of  $\hat{x}$  and the shifts in the pension parameters

$$db = \frac{\tau_R x}{1-x} \cdot \hat{x} + \left[ \frac{1+x}{1-x} - \frac{\partial p}{\partial\tau} \right] \cdot d\tau - \frac{\partial p}{\partial m_0} \cdot dm_0 - \frac{\partial p}{\partial\alpha} \cdot d\alpha. \quad (\text{A.4})$$

This equation corresponds to the PAYG budget locus in Figures 1 and 2. It is upward sloping since an increase in retirement age relaxes the pension budget and allows for a larger flat pension as long as the participation tax rate  $\tau_R$  is positive. This is intuitive since the participation tax measures the net fiscal loss to households, and, thus, the net gain to the system, when retirement is marginally postponed. The tax rate  $\tau_R$  captures the extra tax paid plus the pension earnings foregone minus the increase in pensions over the remaining life-time  $1-x$ , which corresponds to the number of pensioners in the cross-section of the population.

The solution of (A.2) and (A.4) determines the reduced-form, equilibrium expressions for the retirement response and the size of the flat, lump-sum pension payments in terms of the changes in the system parameters  $(\tau, m_0, \alpha)$  and the preference parameter  $\beta$ . This solution yields, in turn, the reactions of the other variables of interest: the response of intensive labor supply of young workers through the impact of retirement age on the implicit tax, as discussed above in (10) and (11). We can also infer the impact on the participation tax of the old, which yields the welfare change according to (24).

## B Effects on the Participation Tax Rate

**Statutory Tax Rate:** Appendix B calculates how pension reform affects the participation tax rate:  $\tau_R = \tau + p - (1 - x)p'$ . To do so, we must compute its partial derivatives for a given retirement date  $x$ . Consider first the effect of an increased contribution rate

$$\frac{\partial \tau_R}{\partial \tau} = 1 + \frac{\partial p}{\partial \tau} - (1 - x) \frac{\partial p'}{\partial \tau}. \quad (\text{B.1})$$

The impact on earnings-linked pensions depends on the reaction of the assessment base,  $z = x + L$ , which, in turn, is driven by first period labor supply in (9). Using  $\tau_L$  as given in (6) and holding  $x$  constant, we find that a higher contribution rate discourages intensive labor supply and thereby erodes the assessment base

$$\tau \frac{\partial z}{\partial \tau} = \tau \frac{\partial L}{\partial \tau_L} \frac{\partial \tau_L}{\partial \tau} = -\frac{\tau_L}{1 - \tau_L} \cdot \sigma L < 0. \quad (\text{B.2})$$

In calculating the effect on pensions  $p = m\tau z + b$ , we note that the conversion factor  $m = \frac{\alpha}{1-x} + m_0$  and its derivative  $m' = \frac{\alpha}{(1-x)^2} = \frac{m-m_0}{1-x}$  are independent of  $\tau$ . A higher contribution rate thus affects the pension level and the pension increment  $p' = \tau \cdot [zm' + mz']$  that is offered when retirement is marginally postponed

$$\frac{\partial p}{\partial \tau} = m \left[ z + \tau \frac{\partial z}{\partial \tau} \right], \quad \frac{\partial p'}{\partial \tau} = m \left[ z' + \tau \frac{\partial z'}{\partial \tau} \right] + m' \left[ z + \tau \frac{\partial z}{\partial \tau} \right]. \quad (\text{B.3})$$

The term  $z' = 1 + L' = 1 - \Psi$ , with  $\Psi \equiv \frac{\sigma L}{1 - \tau_L} \cdot \frac{m_0 \tau}{R}$ , follows from (11).<sup>20</sup> Assuming a fixed wage elasticity of labor supply  $\sigma$ , we obtain

$$\tau \cdot \frac{dz'}{d\tau} = -\Psi \cdot \left[ 1 + (1 - \sigma) \frac{\tau_L}{1 - \tau_L} \right]. \quad (\text{B.4})$$

Using the relationships  $(1 - x)m' = m - m_0 = \alpha/(1 - x)$  and substituting the relevant derivatives into (B.1) yields

$$\begin{aligned} \frac{\partial \tau_R}{\partial \tau} = & 1 - \alpha + m_0 \cdot \left[ z - (1 - x) - \frac{\tau_L}{1 - \tau_L} \sigma L \right] \\ & + (1 - x)m \cdot \Psi \left( 2 + (1 - \sigma) \frac{\tau_L}{1 - \tau_L} \right). \end{aligned} \quad (\text{B.5})$$

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<sup>20</sup>Indeed, we have  $m_0$  and not  $m$  in  $\Psi$ . Moreover, both  $m_0$  and  $m$  are independent of  $\tau$ .

From this general expression, we deduce several cases: full actuarial fairness:  $\alpha = 1$ ,  $m_0 = \Psi = 0$ , and hence  $\partial\tau_R/\partial\tau = 0$ . The zero participation tax rate is independent of the remaining a positive effective tax on young workers,  $\tau_L = \tau \cdot [1 - 1/R]$ , which is smaller than the statutory rate because PAYG contributions earn no interest. The other extreme case is no tax-benefit link,  $\alpha = m_0 = 0$ , so that  $\partial\tau_R/\partial\tau = 1$ .

The case with a fixed conversion factor independent of retirement behavior,  $m = m_0$  and  $\alpha = 0$ , yields an intermediate case. The square bracket can safely be assumed positive, at least if the labor supply elasticity is not too large. In our simple model, the worker-retiree ratio is  $(1 + x) / (1 - x)$ , which exceeds unity in a realistic setting. If, instead, taking the effective number of workers,  $L + x$ , and realistically assuming that hours worked of young and older workers are not too different, i.e.  $L$  close to 1, we also have  $z = L + x > (1 - x)$ . Therefore, the first two terms in the square bracket are clearly positive. A natural assumption, which is actually stronger than required, is that the erosion of the assessment base will not be so large as to exceed the net effect of the first two terms in the square bracket.

It will also be instructive to consider the case of fixed first period labor supply, given by  $\sigma = \Psi = 0$ , which again leads to an increase in the participation tax rate if the statutory tax rate is raised,  $\frac{\partial\tau_R}{\partial\tau} = 1 - \alpha + m_0 [z - (1 - x)] > 0$ ,  $\alpha \in [0, 1]$ . By continuity, the total effect on  $\frac{\partial\tau_R}{\partial\tau}$  remains positive at least for small values of  $\sigma$ . In any case, the influence of  $L$  is likely to be small, given the econometric evidence on the labor supply response of young workers.

**Tax-Benefit Link:** Consider the effect of a tighter tax-benefit link  $m = \alpha / (1 - x) + m_0$ , through a rise in  $m_0$ , starting from  $m_0 = 0$ . The parameter  $\alpha \in [0, 1]$  may take arbitrary values with  $\alpha = 0$  being one special case. The partial effect on  $\tau_R = \tau + p - (1 - x)p'$  is

$$\frac{\partial\tau_R}{\partial m_0} = \frac{\partial p}{\partial m_0} - (1 - x) \frac{\partial p'}{\partial m_0}. \quad (\text{B.6})$$

Using  $\tau_L$  as given in (6), and holding  $x$  constant, we find that a tax-benefit link encourages intensive labor supply and thereby expands the assessment base  $z = x + L$

$$m \frac{\partial z}{\partial m_0} = m \frac{\partial L}{\partial \tau_L} \frac{\partial \tau_L}{\partial m_0} = \frac{\tau - \tau_L}{1 - \tau_L} \cdot \sigma L > 0. \quad (\text{B.7})$$

Raising the conversion factor  $m_0$  affects the pension level,  $p = \tau m z + b$ , and the pension increment  $p' = \tau [m z' + m' z]$  in (16) by

$$\frac{\partial p}{\partial m_0} = \tau \left[ z + m \frac{\partial z}{\partial m_0} \right], \quad \frac{\partial p'}{\partial m_0} = \tau \left[ z' + m \frac{\partial z'}{\partial m_0} + m' \frac{\partial z}{\partial m_0} \right]. \quad (\text{B.8})$$

Since we evaluate the policy change starting from  $m_0 = 0$  in the initial equilibrium, the marginal effect of later retirement on the assessment base is unity,  $z' = 1 + L' = 1$ . Given  $m_0 = 0$  initially, the term  $(1 - x) m = \alpha$  and the effective tax rate  $\tau_L = \tau [1 - (1 - x) m / R]$  remain constant, and therefore, first period labor supply, is independent of retirement age. Consequently

$$\frac{\partial p'}{\partial m_0} = \tau \left[ 1 + m' \frac{\partial z}{\partial m_0} \right]. \quad (\text{B.9})$$

Combining (B.6)–(B.9) and noting that  $m_0 = 0$  implies  $(1 - x) m' = m$ , yields

$$\frac{\partial \tau_R}{\partial m_0} = \tau [z - (1 - x)] > 0. \quad (\text{B.10})$$

When strengthening the tax-benefit link by raising  $m_0$  from an initial value of  $m_0 = 0$ , the partial effect on the participation tax rate reduces to  $\partial \tau_R / \partial m_0 = \tau [z - (1 - x)] > 0$ , where the square bracket can safely be assumed positive as before.

**More Actuarial Fairness:** Raising the parameter  $\alpha$  not only introduces a tighter tax-benefit link, but also makes it fairer. Again, we assume  $m_0 = 0$  initially. The partial impact on the participation tax rate  $\tau_R = \tau + p - (1 - x) p'$  is

$$\frac{\partial \tau_R}{\partial \alpha} = \frac{\partial p}{\partial \alpha} - (1 - x) \frac{\partial p'}{\partial \alpha}. \quad (\text{B.11})$$

Using  $\tau_L$  in (6), and holding  $x$  constant, we find the pension base  $z = x + L$  grows by

$$\frac{\partial z}{\partial \alpha} = \frac{\partial L}{\partial \tau_L} \frac{\partial \tau_L}{\partial \alpha} = \frac{\sigma L}{1 - \tau_L} \cdot \frac{\tau}{R} > 0. \quad (\text{B.12})$$

The conversion factor changes by  $\partial m/\partial\alpha = 1/(1-x)$  and  $\partial m'/\partial\alpha = 1/(1-x)^2$ . The tax-benefit link thus affects the pension level  $p = m\tau z + b$  and the pension increment  $p' = \tau [m'z + mz']$  in (16) according to

$$\frac{\partial p}{\partial\alpha} = \tau \left[ \frac{z}{1-x} + m \frac{\partial z}{\partial\alpha} \right], \quad \frac{\partial p'}{\partial\alpha} = \tau \left[ \frac{z}{(1-x)^2} + m' \frac{\partial z}{\partial\alpha} + \frac{1}{1-x} \right]. \quad (\text{B.13})$$

Our assumption of  $m_0 = 0$  initially implies that  $(1-x)m = \alpha$  does not vary with  $x$ . Later retirement thus expands the assessment base  $z = L + x$  by  $z' = 1$ , with  $\partial z'/\partial\alpha = 0$ . Combining (B.11)–(B.13) yields, upon using  $m = (1-x)m'$

$$\frac{\partial \tau_R}{\partial\alpha} = \frac{\partial p}{\partial\alpha} - (1-x) \frac{\partial p'}{\partial\alpha} = -\tau. \quad (\text{B.14})$$

Consequently, introducing more actuarially fairness reduces the participation tax rate.

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